

5

TRAPPED ION REGIME

$$v_{\perp i}/c < \omega < v_e/c, \quad \omega/k_{\parallel} < (\epsilon T_i/m_i)^{1/2}$$

$$\omega = \omega_j + \sqrt{\epsilon} \omega_{pe}/(1+\tau) + i \epsilon^2 \omega_{pe}^2/v_e (1+\tau)^2$$

STABILITY FOR +VE FEEDBACK

$$\text{PHASE } 180^\circ \text{ GAIN: } \epsilon^2 \omega_{pe}^2/v_e (1+\tau)^2$$

5

$$n^+ - n^- = \frac{1}{2} \sqrt{\epsilon_0} n(r) \sqrt{\rho} (\cos \theta + \sqrt{1 - a^2})^{1/2}$$

$$\left[\exp\left(-\lambda \frac{\pi - \theta_m - \theta}{\cos \theta + \sqrt{1 - a^2}}\right) - \exp\left(-\lambda \frac{\pi - \theta_m + \theta}{\cos \theta + \sqrt{1 - a^2}}\right) \right]$$

where a is the solution of

$$\left(\frac{2\lambda}{a} - 1\right)(\cos \theta + \sqrt{1 - a^2}) = 2\lambda(\pi - \theta_m - \frac{a}{|a|}\theta)$$

7

TABLE II

Experiment	Scaling	v_g (a)	Ω (eV)	β_0	v_g (v)
FLT	A	0.23	1400	0.28	0.75
$R = 1.3 \text{ m}, \mu = 0.45 \text{ m}$	B	0.08	900	0.19	1.45
$I = 1 \text{ MA}, n_p = 10^{20} \text{ m}^{-3}$	C	0.024	500	0.12	3.0
JET	A	1.65	1300	0.30	0.59
$R = 2.96 \text{ m}, \mu = -1.25 \text{ m}$	B	0.15	400	0.11	3.0
$I = 2.6 \text{ MA}, n_p = 10^{20} \text{ m}^{-3}$	C	0.014	190	0.04	12

4

COLLISIONLESS REGIME ($T_i = T_e$)

$$(\omega - \omega_f)^2 = \omega_M^2 + \sqrt{\epsilon} \omega_* \omega_M \quad (\omega_* \omega_M < 0)$$

$$(\omega_M \cong CT/eBR, \omega_* \cong CT/eBR.)$$

STABILITY FOR +VE FEEDBACK

$$\text{PHASE } 180^\circ \text{ GAIN: } \epsilon^{1/4} \|\omega_* \omega_M\|^{1/2}$$

4

$$n_T = \frac{1}{\sqrt{\pi}} \left(\frac{1}{T}\right)^{1/2} n(r) \int \frac{B d\mu dE}{\sqrt{|E - \mu B - q\Phi|}} e^{-E/T}$$

$$= \frac{n(r)}{T\sqrt{\pi}} \int_{\mu_{\min}}^{\infty} B d\mu e^{-[\mu B + q\Phi]/T} \left\{ x_{\max} e^{-x_{\max}^2} - x_{\min} e^{-x_{\min}^2} \right\}$$

$$x_{\max}^2 = e\lambda \left[\frac{\mu}{\mu_m} (\cos \theta - \cos \theta_{\max}) + \frac{q}{|q|} (\theta - \theta_{\max}) \right]$$

$$\lambda = \mu_m B_0 / T$$

7

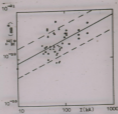
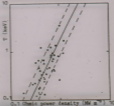


Fig. 3. Type B scaling



0.1 Ohmic power density (MW m^{-2}) 10

Fig. 4. Type C scaling

2

ENERGY OF TRAPPED PARTICLES

$$E = \frac{1}{2} m v_{\parallel}^2 + \mu B + q\phi$$

PARTICLE TRAPPED IF

$$E < (\mu B + q\phi)_{\max} \rightarrow \left[\begin{array}{l} \text{lower maximum} \\ \text{of potential} \end{array} \right]$$

MAXIMUM AND MINIMUM OF $(\mu B + q\phi)$ FOR
A GIVEN μ OCCUR AT

$$\theta_{\min} = \sin^{-1}(qE_0 R_0 / \mu B_0)$$

$$\theta_{\max} = \pi - \theta_{\min}$$

SOURCE TERM

$$S_F = -i\omega_f \tilde{n}_k \quad (\text{FLUID THEORY})$$

$$S_K = -i\omega_f \tilde{n}_k \delta(v_{||}) \delta(v_{\perp} - v_b) \delta(\psi) / 2\pi v_{\perp}$$

(KINETIC THEORY)

GAIN: AMP(ω_f) PHASE: ARG(ω_f)

$\omega_f > 0$ -VE FB & VICE VERSA

3

FOR $\mu = \mu_{\min} = 4R_0 E_0 / B_0$.

$$\theta_{\min} = \theta_{\max} = \pi/2$$

NO TRAPPING FOR $\mu < \mu_{\min}$



6

TRAPPED ELECTRON REGIME

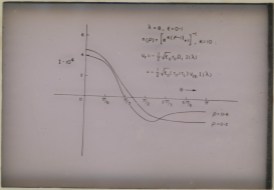
$$\omega_{pe} < v_e/\epsilon, \quad (\epsilon T_i/m_i)^{1/2} < \omega/k_y < (\epsilon T_e/m_e)^{1/2}$$

$$\omega_R \approx \omega_{pe}, \quad \gamma = \frac{\epsilon}{v_e} \left\{ \omega_{pe} (\omega_i^2 + \omega_{pe}^2) / (1 - \epsilon \frac{\omega_i^2}{v_e^2}) \right\}$$

STABILITY

	+VE FB	-VE FB
PHASE	90°	0°
GAIN	$\sim \omega_{pe}$	$\sim v_e/\epsilon$

7



7

TABLE I

Experiment	Main parameters				Symbol on Graphs	References
	$R(a)$	$a(a)$	$I(kk)$	$a_0 (10^8 \text{ m}^{-2})$		
ES and ESa	1.0	0.1-0.15	36-90	0.3-2.7	A	1,2
TS	1.0	0.17	110-180	1.0-3.0	o	3,4
ST	1.09	0.06-0.74	10-100	0.5-3.3	□	5,6,7,8,9
AYE (uncomp ^d)	0.88	0.17	60-80	0.6-2.1	*	10,11
OMMA	0.8	0.23	95-160	1.2-2.0	*	12,13
CLEO-Tokamak	0.9	0.12-0.18	34-72	1.0-2.4	x	14
TFR	0.96	0.17-0.2	103-300	1.6-3.5	•	15,16
POLARIS	0.7	0.12	44	1.1	•	17
ALCATOR	0.56	0.10	190	1.3	v	18

6

$$= 8\pi q r_0^2 \int_0^1 \rho' d\rho' \int_{-\pi}^{\pi} d\theta' (1 + \epsilon_0 \rho \cos \theta)^{-1/2} (1 + \epsilon_0 \rho' \cos \theta')^{-1/2}$$

$$Q_{-1/2} [\xi(r, r', \theta, \theta')] [n^+(r', \theta') - n^-(r', \theta')]$$

$$\text{where } \xi = 1 + \frac{1}{2} \epsilon_0^2 \frac{\rho^2 + \rho'^2 - 2\rho\rho' \cos(\theta - \theta')}{(1 + \epsilon_0 \rho \cos \theta)(1 + \epsilon_0 \rho' \cos \theta')}$$

$$\epsilon_0 = \frac{r_0}{R_0}, \quad \rho = \frac{r}{r_0}, \quad \rho' = \frac{r'}{r_0}$$

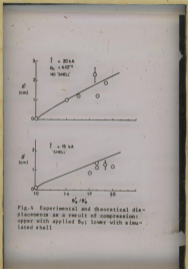


Fig.4 Experimental and theoretical displacements as a result of compression: upper with applied D_0 ; lower with simulated shell

7

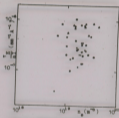


Fig. 2. Type A scaling.



FLUID THEORY



KINETIC THEORY

$$\vec{B} = B_0 \epsilon \cos(\eta) \hat{e}_\theta + B_0 (1 + \epsilon \eta \sin(\theta)) \hat{e}_z$$

$$\epsilon = r/R, \quad \eta(\theta) = \text{Sgn}(\cos\theta)$$

GEOMETRY

POLARIZATION OF
TRAPPED PARTICLES IN A
TOKAMAK

$$V_r = -\frac{eE_\theta R}{\Omega^2} \hat{e} \text{ IS RADIIALLY INWARDS}$$



$$\Phi = -\int dV = -\frac{eB_\theta E_0}{\Omega^2} (\theta + 2\epsilon \sin \theta)$$

$$B_\theta = B_0 (1 + \epsilon \cos \theta)^{-1} \hat{e} = r/R_0$$

BASIC EQUATIONS

$$\frac{\partial n}{\partial t} + \nabla \cdot (n\vec{v}) = S$$

$$\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \nabla) \vec{v} = \frac{e}{m} (-\nabla \phi + \vec{v} \times \vec{B}_0) - \frac{1}{mn} \nabla (nT)$$

$$(\tilde{n}_t + \tilde{n}_u)_e = (\tilde{n}_t + \tilde{n}_u)_i$$

FOR UNTRAPPED PARTICLES

$$\tilde{n}_u = n_0 (1 - \sqrt{\epsilon}) e\phi/T$$

119

(6)



Figure 1. Regions of magnetostability in velocity space as seen on the outside of the torus.

I

TABLE III

I (kA)	96	145	200	303
V (volts)	1.85	1.85	1.75	1.88
q (a)	10	7	4.8	3.3
$N_e I$ (10^{15} cm^{-2})	1.07	1.25	1.88	2.61
w_e (J/cm)	2.7	5.4	8.1	13
w_i (J/cm)	1.6	3.1	4.5	8
δ	0.62	0.54	0.42	0.3
Z_{eff}	3.6	4.2	2.7	3.55
τ_E (ms)	15	19.5	22	22.7

from Tables I & II

7

KINETIC EFFECTS

INCLUSION OF MOMENTUM SOURCE &
FLR CORRECTIONS - ALL DISSIPATIVE
INSTABILITIES SIMULTANEOUSLY
SUPPRESSED WITH -VE FB

PHASE -90° GAIN $\sim 2v_e^0 / 3 \epsilon^0 \eta_e \omega_{pe}$

112

$$= -h^2 \frac{\partial^2}{\partial x^2} - \frac{2\alpha h}{h^2} \frac{\partial}{\partial x} \quad (5)$$

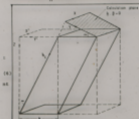


Fig. 1 Slab model with periodic 'toroidal' (x) and 'poloidal' (y) directions. With a rational surface, the field varies in one of the planes containing a wave-number.

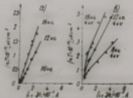


Fig. 1. α, β (L.E.J.) dotted line corresponds to Artasovich's formula with $C^2 = 5$.

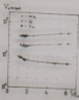


Fig. 2. $n = 3 \times 3 \cdot 10^{13}$
 $\beta = 16 \text{ EG}$



Fig. 3. $n = 10^{12} \text{ cm}^{-3} - 2 \cdot 10^{13}$
 $\beta = 16 \text{ EG}$

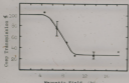


Fig. 1. Coep Transmission

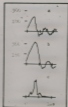


Fig. 2. Diode voltage vs. t , a without and b with iron collar; c

92

Machine	100 kV Maxx	500 kV, 7 Ω Blumlein	150 kV Blumlein	5 MV CREB
Ion Energy	~ 100 keV	500 keV	150 keV	2 MeV
Ion Current	2 x 250 A	2 x 7,000 A	2 x 3,500 A	~ 5,000 A
Pulse Width	~ 50 nsec	~ 50 nsec	~ 50 nsec	< 50 nsec
Current Density	~ 10 A/cm ²	0.5 A/cm ²	~ 10 A/cm ²	~ 50 A/cm ²
Efficiency %		9%	4%	
Type of ions	proton	proton	proton	proton & Al ¹³⁺

TABLE 1 - $\eta = \text{Proton Energy/Total Energy Input}$ [Vidt]

412

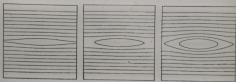


Fig. 1. The non-linear evolution of an island state (left to right) for a symmetric Gaussian distribution. The final equilibrium state ($\delta E = 0$) is illustrated on the right.

C. Example of Solutions. The non-linear development of the instability, with the final island state ($\delta E = 0$) is illustrated in Fig. 2.

75

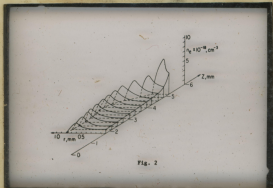


Fig. 2

plasma in a field of 19.4 kG. The ~30% axial density minimum is much more than

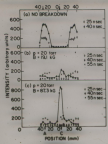


Figure 1

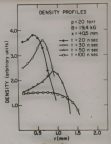
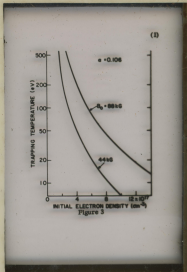


Figure 2

77



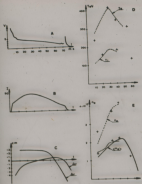


Fig. 1 - a typical discharge, b low voltage, c plate current,
 d total and useful displacement, e electric and ion temperature,
 f experimental results (Thomson electron density and higher ionization of
 Fig. 1000), g peak and average electron densities - Thomson scattering
 results, h after low γ ion interference.
 In a and c, dotted lines are discharge simulation results.

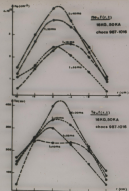
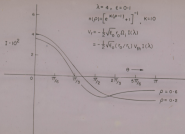


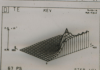
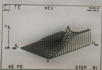
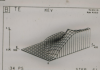
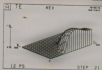
Fig. 1 - Radial profiles of electron temperature and density along a vertical chord at $R = 70$ cm.

8



71

SIAMM_3



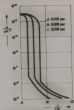


Fig. 4. Development of plasma density in time. Same like in Fig. 3.

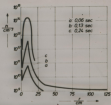


Fig. 5. Development of plasma density in time. Same like in Fig. 3.

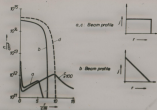


Fig. 11. Plasma density distribution after 0.24 sec of injection.

- a. Beam with 1 cm radius, constant current density j .
- b. Beam with 1 cm radius, current density j peaked on the axis.
- c. Beam with 10 cm radius, constant current density j .
- d. Parabol beam (beam γ of (11)).

netic field on both particles and (particle) energy.

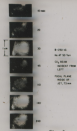


Fig. 3

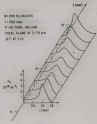


Fig. 4

75

He at 50 torr, $B = 90 \text{ kG}$

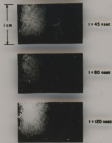
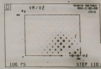
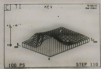
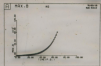


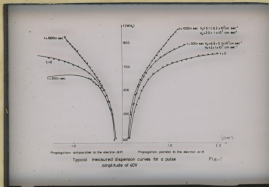
Fig. 1

70

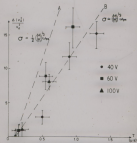
Figure 1



165



165



Estimation of the electrical conductivity, σ , from the electron heating rate
Fig. 5

171

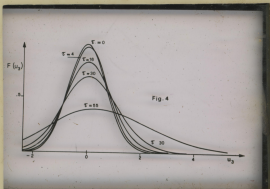


Fig. 5. Behavior of $|E|$ inside the plasma
 a) $|E|$ for the (1,0) resonance b)
 $|E_x|$ and $|E_y|$ for the (0,1) resonance.



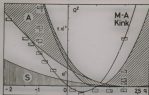


Fig. 1. Low-frequency part of the real spectrum of a micro-lens. S = absolute continuous, A = discrete continuous, single isolated region = one singularity, doubly isolated region = two singularities, M-A = non-symmetric. The lateral kink is barely stable between $q=1$ and $q=0.5$. The real component of the eigenvalue is shown in the rectangle, the center being on the left.

Fig. 2. Real component of the eigenvalue normalized to the boundary value, for values of q on both sides of the merging point. At $q=1.0$ the kink has already reached the continuum.



158



Fig. 1

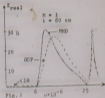


Fig. 2

Main results of our experiments are given in figures.

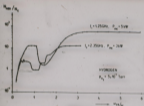


FIG. 1

Fig. 1 shows the dependence of a mean electron density N_{mbe} of the hydrogen plasma created after absorption of the microwave power with frequency $f_1 = 1.25 \text{ GHz}$ and $f_2 = 2.35 \text{ GHz}$ in the initial plasma on the magnetic field H_0 . Since the degree of ionization of our initial plasma was very small ($\approx 1\%$) and practically all the absorbed energy went into neutral gas ionization,

154

by nonlinear wave-wave interaction

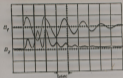


Fig. 1: B_1 and B_2 at $r = 3$ cm

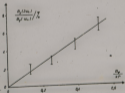


Fig. 2: Amplitude of double frequency B_2 as a function of B_1

In the low amplitude case, the Alfvén



Fig. 3. Slab with coordinate systems ($-a$ and a correspond to $w_{22}^{(2)}$ and $w_{22}^{(1)}$).

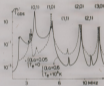
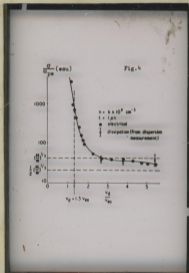
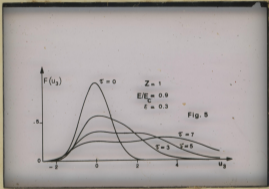


Fig. 4. $\text{Im}(k)$ for an inhomogeneous slab with $\alpha = 0.05$ and $\alpha = 0.36$. The dots indicate where $\text{Re}(k) = \alpha$ coincides with $\alpha = 0$.



171



144

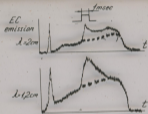
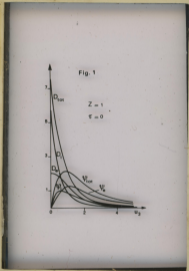


Fig 2
Reference

171



164

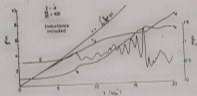
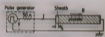


Fig. 4

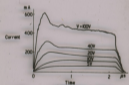
165



$$V = V_s + R_p I = 50I$$

$$V_s = I^2 R$$

(a) Schematic arrangement of the experiment



(b) Measured current Fig. 1

153

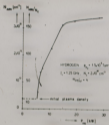


FIG. 3

144

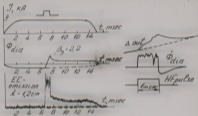


Fig 1

155

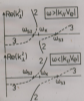


Fig. 1. k_{12}^2 and k_{21}^2 versus u .

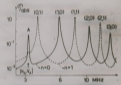


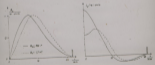
Fig. 2. Spectra for $\nu=0$ and $\nu=1$ in the homogeneous cylindrical case (radius $a=1$, $T_a=0$).

154



Fig. 3:
Sampling constant 2
 10^4 and 10^3 ; as a
function of the
amplitude A_0

Fig. 4:
Normalized radial
amplitude profile A_r
and normalized current
density J_z for two
different wave ampli-
tudes.



153

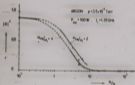


FIG. 2

- (1) at $\omega/\omega_c \ll 1$ the reflection is high and the system slow down structure - plasma represents for the incident wave practically a short circuit;

radial direction to the ion ring a linear phase shift. In a similar manner the phase shift corresponds to a phasevelocity of 8×10^3 m/s in the longitudinal direction.



Fig. 3 Dispersion of perpendicular propagating ion cyclotron waves in a plasma with a velocity distribution which consists of a mixture of a Maxwellian and a δ -function. Low B -field case.

184

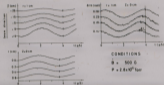


Fig. 2 A typical set of cw wave propagation measurements. In axial or radial direction we do not find a clear phase shift. In azimuthal direction the phase shift corresponds to a phase velocity of 8×10^3 m/s in the direction of gyration.

CONDITIONS B=500 G

WAVE

= gyration direction.

185

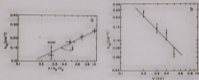


Fig. 3: (a) Beam density dependence ($V_b = 200$ V), and (b) Beam energy dependence ($n_b = 10^{18} \text{ cm}^{-3}$) of the spatial growth rate $B = 4$ kG, $n_p = 2 \times 10^{20} \text{ cm}^{-3}$.

181a

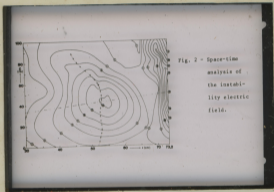


Fig. 2 - Space-time
analysis of
the instabi-
lity electric
field.

181

(a)

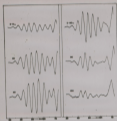


Fig. 1 - "Instantaneous pictures"
of the bursts in space.

184

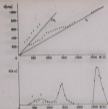
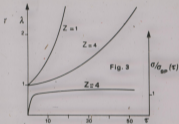
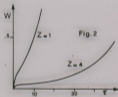


Fig. 1 Dependence of instability frequency and amplitude on the magnetic field.

171



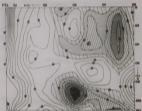
171

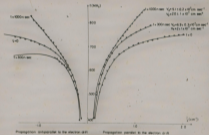


181

(a)

Fig. 3 - Space-time analysis
of the plasma
"density". Darker
areas represent
higher "densities".





Typical measured dispersion curves for a pulse
 amplitude of 12V

Fig. 2

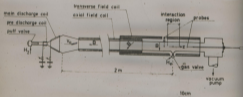


Fig. 20. Experimental arrangement of Danilovson (1969).

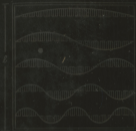
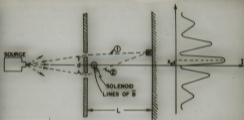


Fig. 23-1. A cross-section of "Jean's cube," showing the different waves that can exist inside it. Only the waves propagating in a horizontal direction are shown here. The block that is a few centimetres.



A magnetic field can influence the motion of electrons even though it exists only in regions where there is an arbitrarily small probability of finding the electrons.

if $n \Delta \bar{e} = dU$, change in internal energy

$$n \bar{v} = p , A \delta l = \delta V$$

and if

$$\delta Q = nV \delta \eta$$

then

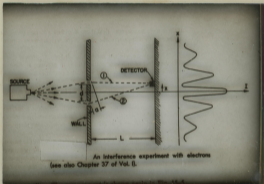
$$dU = \delta Q - p \delta V, \Rightarrow \text{1st Law}$$

New Definitions of Heat and Work:

Work: All that energy added adiabatically

Heat: All that energy added nonadiabatically.

< generalized definitions of heat,



JET

Experimental Programmes:

Phase I: (Starts 1980) 2-3 years

- (a) establish a range of operating conditions
- (b) perform scaling studies
- (c) work upto the maximum of plasma current for the installed power supplies including the use of D-shaped cross-section.
- (d) examine additional heating without internal structures.
- (e) investigate impurity effects
- (f) establish the limits of operation
- (g) decide on future power supplies
- (h) decide whether divertor is needed

185



Fig. 1: Schematic of Q-machine and ion beam setup.



Fig. 2: Frequency spectrum of the mode amplitude.
 $B = 4.65 \text{ kG}$, $n_D = 3 \times 10^{16} \text{ cm}^{-3}$