

THIS BOOK BELONGS TO

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CLASS OF \_\_\_\_\_

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To

Toshi

from

Anan<sup>14</sup>

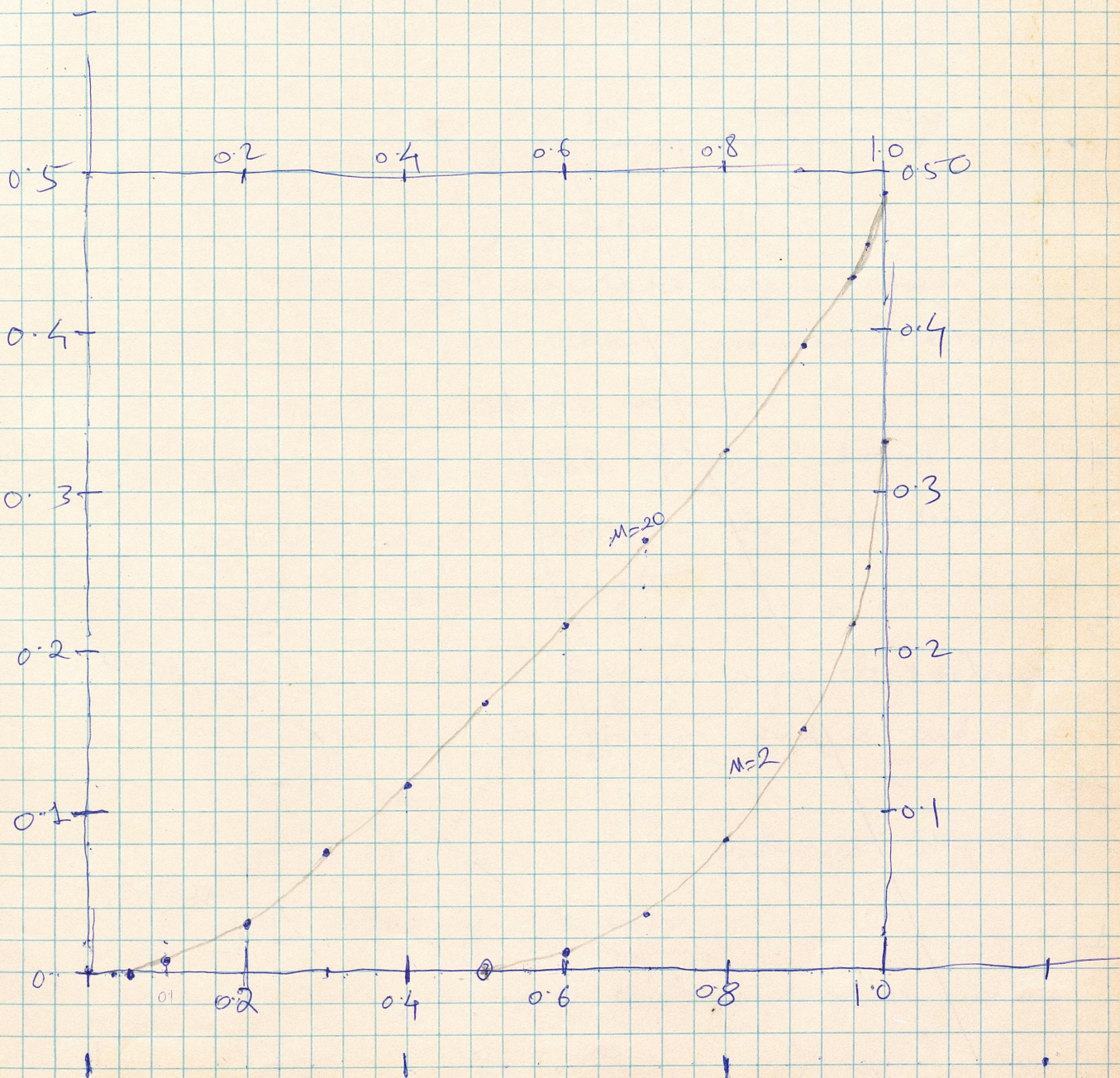
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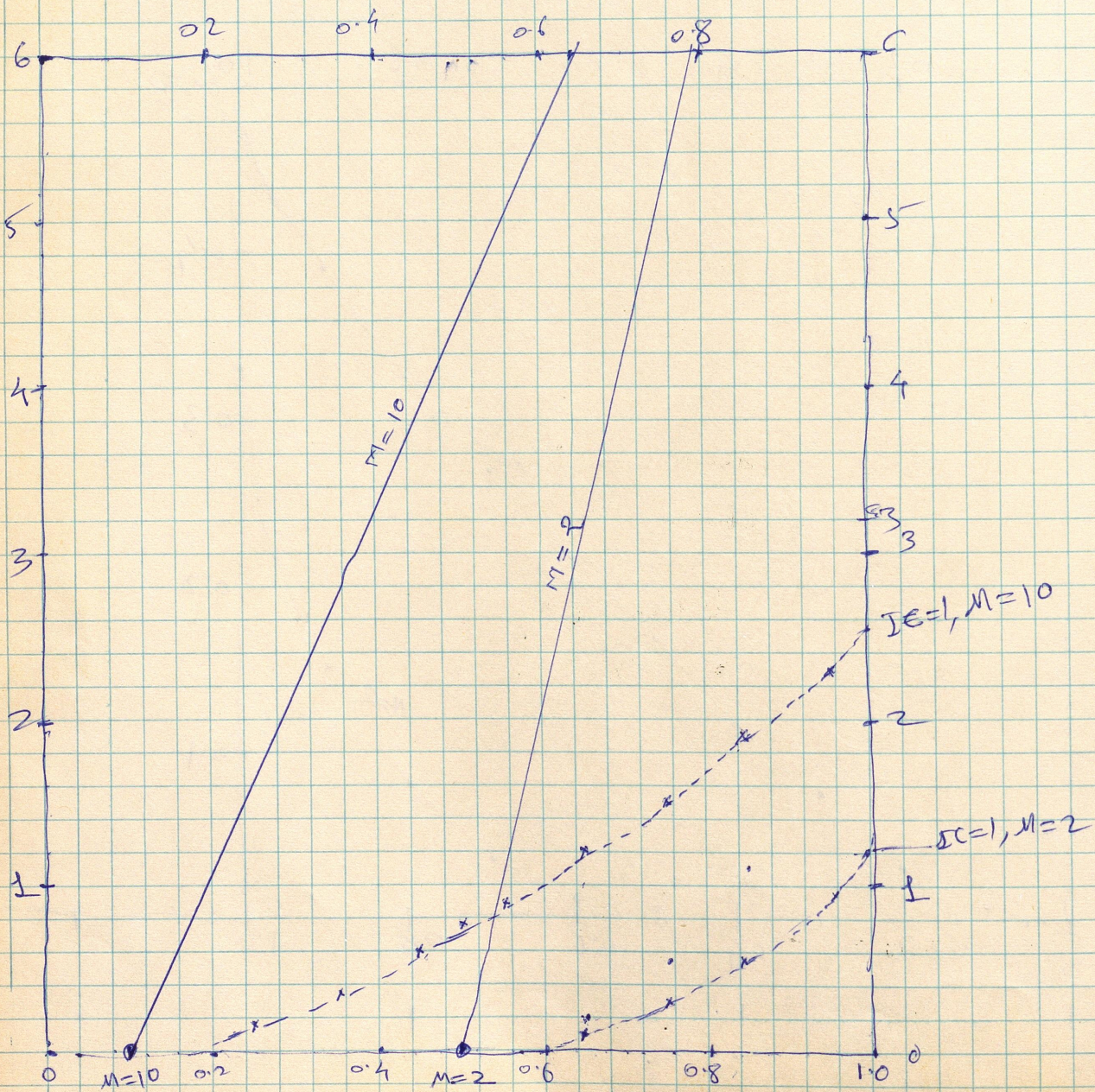


31/1/85

$N=3$   
 $n=20$



3/2/85  
 $n=4$



# Physical Chemistry of Macromolecules

C. Tanford.

## ch. 3: Statistics of Linear Polymers.

Molecular wt. averages and Distributions

- B. a) degree of polymerization and molecular weight  
 b) Molecular wt. distributions  
 c) fractionation of polymers  
 d) M-wt. average  
 e)

Average dimensions

- a) Average end to end distance  
 b) Average radius of gyration  
 c) The completely unrestricted polymer chain  
 d) the polyethylene chain, assuming free rotation  
 e) The effect of restricted rotation  
 f) Other simple flexible polymer chains  
 g) general ideal expression for dependence of  $\bar{r}_{av}$  on chain length  
 h) Interaction betw. polymer segments & solvent molecules and its effect on end to end distances  
 i) completely rigid chain polymers. Stiff chain  
 j) The radius of gyration  
 k) Application to heterogeneous polymer mixtures  
 l) Non-linear polymers

10. Distribution functions for Polymer Configuration

a) The problem of random flight

b) Distribution function for end to end distances

c) Distribution of segments relative to centre of mass

Important relations

$$M_x = x M_0 \begin{matrix} \nearrow \text{no. of repeating units} \\ \text{or degree of polymerization} \\ \downarrow \\ \text{residue (unit) molecular wt} \end{matrix}$$

no. average DP

$$\bar{x}_n = \frac{N_0}{N_0 (1-p)} \rightarrow \text{extent of reaction}$$

$$= \frac{1}{1-p}$$

$$M_n = \frac{\sum N_i M_i}{\sum N_i} = \sum x_i M_i$$

M<sub>n</sub>

$$= M_0 \sum_{x=1}^{\infty} x X_x$$

$$\bar{x}_n = \frac{\sum_{x=1}^{\infty} x N_x}{\sum_{x=1}^{\infty} N_x} = \sum_{x=1}^{\infty} x X_x$$

$$\bar{M}_w = \frac{\sum g_i M_i}{\sum g_i} = \sum w_i M_i$$

$$\bar{x}_w = \frac{\sum_{x=1}^{\infty} x^2 N_x}{\sum_{x=1}^{\infty} x N_x} = \frac{\sum x_i N_i^2}{\sum x_i}$$

Average end to end distance (~~end~~)

$$h_{av} = \sqrt{\overline{h^2}} \quad \text{distance betw. ends}$$

$$= \left( \overline{h \cdot h} \right)^{1/2}$$

Ave. radius of gyration:  $R^2 = \frac{\sum_i m_i r_i^2}{\sum_i m_i}$

(square root of the wt. average  $r_i^2$  for all mass elements)

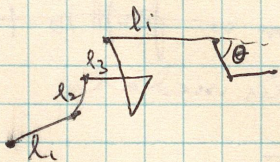
$$R_g = \left( \overline{R^2} \right)^{1/2} = \left( \frac{\sum_i m_i r_i^2}{\sum_i m_i} \right)^{1/2}$$

$$= \left( \frac{\sum_i m_i \overline{r_i^2}}{\sum_i m_i} \right)^{1/2}$$

$$= \left( \frac{\sum_i \overline{r_i^2}}{\sigma} \right)^{1/2}$$

where  $\sigma$  is total no of mass elements per chain  
(if mass elements are identical  
ie  $\sigma = \frac{\text{total mass } (\sum m_i)}{\text{mass of element } (m_i)}$ )

① For completely unrestricted polymer chain



$$\overline{h^2} = \sum_{i=1}^{\sigma} l_i^2 = \sigma l^2 = \sigma l_{av}^2$$

② Free rotation but fixed angle: polymethylene chain



$$\overline{h^2} = \sigma l^2 \frac{1 + \cos \theta}{1 - \cos \theta} = 2.000 \sigma l^2$$

for polymethylene  
( $\cos \theta = 0.333$ )

③ General ideal expansion for  $R_{av}$

$$\overline{h^2} = \beta^2 \sigma$$

↳ const. characteristic of the nature of polymer

$\beta = 2^{1/2}$  law for polynucleotides

$\approx 3$  law for synthetic org. polymers

$\beta$  law is measure of stiffness of polymer chain

e) In the case of interaction with solvent:

$$\overline{R^2} = \alpha^2 \overline{R_0^2} = \alpha^2 \beta^2 \sigma \quad (= \alpha^2 \beta^2 M/M_0)$$

$\alpha > 1$  for good solvent

$< 1$  for poor "

$= 1$  for ideal solvent

$\alpha = \text{constant}$

max. variation with M  $\alpha = (\text{constant}) M^{0.1}$   $\overline{R^2} \propto \beta^2 M^{0.6}$

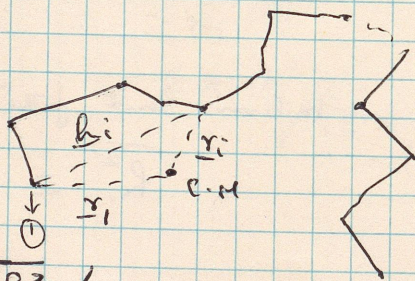
f) Completely rigid chains. Stiff chains.

$$R_{\text{avr}} = (\text{const}) M^{0.5-0.6} \quad \text{for flexible chain}$$

$$= (\text{const}) M^{1.0} \quad \text{for stiff chain}$$

$$= (\text{const}) M^{0.6-0.99} \quad \text{for intermediates}$$

g) Radius of gyration



$$\underline{R_g^2 = \overline{R^2} = \frac{R^2}{6}}$$

for ideal soln.

Distribution function.

$$W(h) dh = 4\pi \left( \frac{3}{2\pi\sigma^2 L^2} \right)^{3/2} e^{-\frac{3h^2}{2\sigma^2 L^2}} h^2 dh$$

$$W(h) dh = 4\pi \left( \frac{3}{2\pi h^2} \right)^{3/2} e^{-3h^2/2h^2} \cdot h^2 dh$$

## Theories of the helix-coil Transitions for Random Copolymers.

Poland + Scheraga.

### Important Points

- Physical insight into the behavior of a random copolymer in the transition region provided.
- Show that an important feature detg. the shape of the transition curve is the variation in composition over the correlation length.

Model: Monomers A & B ; overall composition of A is  $f_A$  ; Random, unknown occurrence of A & B  
only h & c states.

the Temperature of Some Organic Solvents  
 Physical Tables VI-3, p 28-30, 1928

terms of the equation

$$\gamma + 10^{-6}\beta(t-t_0)^2 + 10^{-9}\delta$$

subscript in

has not been

arrived at

in this and

PHYSICO-CHEMICAL  
 AND  
 BIOCHEMICAL  
 DATA

5

0.40

0.45 100

0.0002 0 to 74

110.9 0.001 0 to 156

586 J. Ind. Chem Soc 43, 179 (1966)

$$5 + 0.0009647(T-25)$$

between 30 + 90°C

Equation is VSA's from plot  
 $\frac{d}{dt}$  vs  $T$

66

2014  
~~2010~~  
 1.2825  
 .071  
 ---  
 DCB 1.261  
 d 25 .007  
 ---  
 DCB 0.004x70  
 70 .0130  
 ---  
 1.287  
 .098  
 ---  
 1.85

W

12/2/74

CRC III

## Density change with Temperature of Some Organic Solvents

From International Critical Tables Vol. 3, p. 28-30, 1928

Table below gives the parameters of the equation

$$d_t = [d_s + 10^{-3}\alpha(t-t_s) + 10^{-6}\beta(t-t_s)^2 + 10^{-9}\delta(t-t_s)^3] \pm 10^{-4}\Delta$$

Except when indicated by giving  $t_s$  as a subscript in column 3  $t_s = 0^\circ$ . Where density at  $0^\circ\text{C}$  has not been determined a value has in many cases been arrived at by extrapolation. Such values are given in parenthesis and are given as a basis for calculation only.

Formula	Name	$d_s$	$\alpha$	$\beta$	$\delta$	Limit of error	Range $^\circ\text{C}$
$\text{CCl}_4$	Carbon tetrachloride	1.63255 <del>1.435</del>	-1.9110	-0.690	-	0.0002	0 to 40
$\text{CHCl}_3$	Chloroform	1.52643	-1.8563	-0.5309	-8.81	0.0001	-58 to +55
$\text{C}_2\text{H}_2\text{O}_2$	Formic acid	1.2441	-1.221	+0.126	-	0.002	0 to 40
$\text{C}_2\text{H}_2\text{Cl}_2\text{O}_2$	Dichloroacetic acid	(1.5919)	-1.375	-	-	0.002	0 to 100
$\text{C}_2\text{H}_4\text{Cl}_2$	Ethylene chloride	1.28248	-1.4217	-0.933	+2.29	0.0002	0 to 74
$\text{C}_2\text{H}_6\text{O}_2$	Ethylene Glycol	1.1257	-0.5713	-2.766	+10.9	0.001	0 to 136

DMP

DMF

Chem

Anthracene  
purity  
d vs diff. T's.K<sub>th</sub> must be for

Data of Gopal & Rigby J. Ind. Chem Soc 43, 179 (1966)

$$d_t = 0.9445 + 0.0009647(T-25)$$

between 30 + 90  $^\circ\text{C}$

Equation is VSA's from plot of  $d$  vs  $T$ .

From Glasstone 'Physical Chemistry'

p. 524

Electric moment  $m = \alpha F$ ,  $\alpha$  - polarizability  $F$  - Electric field strength

$$I = m n \quad n \rightarrow \text{no of molecules/cc}$$

From Electrostatics  $E_0 = E + 4\pi I$  or  $(\epsilon - 1)E = 4\pi I$

( $\epsilon$  is dielectric const =  $\frac{E_0}{E}$ )

$$F = E_0 + \frac{4}{3}\pi I - 4\pi I \quad \text{for molecules in spherical cavity}$$

$$= \left(\frac{\epsilon + 2}{3}\right) E$$

$$\therefore \frac{\epsilon - 1}{\epsilon + 2} = \frac{4}{3}\pi n \alpha$$

$$n = \frac{N P}{M} \quad P \text{ is density}$$

$$\frac{\epsilon - 1}{\epsilon + 2} \cdot \frac{M}{P} = \frac{4}{3}\pi N \alpha = P$$

$$\text{or } P = \frac{\epsilon - 1}{\epsilon + 2} \cdot \frac{M}{P} \quad \text{molar polarizability}$$

$$P \leftarrow \frac{\epsilon - 1}{\epsilon + 2} \cdot \frac{M}{P} = \frac{4}{3}\pi N \alpha \quad (\epsilon = n^2)$$

Electric field  $E$  in the visible region, away from absorption bands

p. 519 Lorentz & Loreng found:

$$[R] = \frac{n^2 - 1}{n^2 + 2} \cdot \frac{M}{P} \quad \text{from electronic & wave theories of light}$$

where  $R$  is molecular refraction. (or molar refraction)  
 $R$  is both additive & combinative

Sample calculation for  $H_2O$ :

$$\frac{[R]_{25^\circ}}{M} = \frac{(1.334)^2 - 1}{(1.334)^2 + 2} \cdot \frac{1}{0.99987}$$

Data:  $n_D^{0^\circ} = 1.3340$   $n_D^{70^\circ} = 1.3252$   
 $\rho^{0^\circ} = 0.99987$   $\rho^{70^\circ} = 0.97781$

R-I - density relation for CCl<sub>4</sub> given by

$$\rho^{25^\circ} = (10.8601 \times R^{25^\circ}) = 13.4974, \quad \text{J. Phys Chem 65, 1138 (1961)}$$

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Refractive Index Data

CRC Handbook gives <sup>1968</sup> R.I. dispersion <sup>p. J-240</sup> for  $\text{CCl}_4$ , chloroethanol,  $\text{CHCl}_3$ , cyclohexane, DCA, DMF, p-dioxane, EDC, Ethylene glycol, glycol-water (1:1), formamide, formic acid, furan, hydrazine, methylene chloride, urea.

Concn dependence of R.I. for,  $\text{LiBr}$ ,  $\text{NaCl}$ , urea Refs. J238, 239,  $\text{SnH}_4$ , J241

CRC II

Refractive Index Change with Temperature

check  
concn.  
ref.

Ethanol: Data of Hall & Payne, Phys Rev 1922, 20, 249.  
given by J.R. Partington, <sup>An</sup> Adv. Treatise on  
Physical Chem, IV, p. 30, 1953.  
(Longmans)

$$n_{\text{EtOH}} = n = 1.3625 - 10^{-6} [404(t-15) + 0.22(t-15)^2 + 0.0075(t-15)^3]$$

12/12/74 → (Also see Hawkes & Astheimer J Opt Soc Amer. 1948  
(35, 617, 804)  
(35; not for EtOH but for ~~Et~~)

CRC IV

Chemical Resistance and other properties

- (a) Millipore filters copy pp. 1A050 & 6A010, 6A011 of Catalog of Millipore
- (b) Ultracentrifuge centerpieces.

Three types of <sup>materials</sup> centerpieces are available for <sup>inserts</sup> the Beckman Model E ultracentrifuge.

For use with the Beckman Model E ultracentrifuge, the centerpieces are offered in three materials - Epon (Regd. trademark of Shell Chemical Corp.), Kel-F (Registered trademark of 3M Company) and aluminium. The materials vary in chemical resistance, temperature tolerance and strength. Configuration also affects the strength of the centerpiece as reflected in the maximum speeds of recommended in the chart <sup>given</sup> below.

Chemical Resistance and other properties of ~~analytical ultracentrifuge~~ centrifuge materials 105  
(Registered trademark of SMI Company)

Kel-F : Kel-F is a trifluorochloroethylene polymer.

It has a durometer hardness of 80 (D scale), does not absorb water and is not affected by sunlight. The chlorine constitutes exceptional rigidity of the material, while the fluorine is responsible for its chemical inertness and zero moisture absorption. Because Kel-F is chemically inert, it will withstand exposures to strong acids and alkalis and to most organic solvents.

Kel-F centrifuge pieces are recommended for biological materials — when non-aqueous solvents are to be used or when the pH of the solution falls outside the range tolerated by the Epon centrifuge piece (see below). Notable exceptions are highly halogenated and aromatic compounds.

If Kel-F absorbs certain highly halogenated and aromatic compounds, it will swell slightly. Consequently, when using a Kel-F centrifuge piece with these materials, rinse it immediately after run with distilled water. The following is a partial list of materials that will cause a weight change in Kel-F of 1% or more in seven

days at 25°C.

Chlorine - - -	12.3%
Diethylamine - -	1.9%
Ethyl acetate - -	1.2%
Ethyl ether - - -	3.8%
Ethyl propionate -	1.0%
Freon 113	1.3
Furan	2.4
Methyl acetate	1.0
Methylal	1.3
Methyl ether	6.4
Methyl propionate	1.4
Trichloroethylene	2.3

High speeds may cause a slight distortion in Kel-F centre pieces; the distortion may lead to convection in the cell. Generally, this distortion is negligible but becomes permanent and significant after the centre piece has been used in about 100 runs at maximum speed.

The maximum operating speed of Kel-F centre piece varies as follows; for single sectors - maximum speed of rotor, for double sectors - 6000 rpm, in ~~exception~~ for 6-channel equilibrium ~~centre piece~~ - 20,000 rpm and for

ALUMINUM

10

10

10

10

10

10

10

10

10

10

10

10

10

10

10

10

10

10

fixed path - 30,000 rpm. The maximum operating temperature for Kef Centrifuges is 40°C.

(Registered trademark of Shell Chemical Corporation)

Filled-Epon Centrifuges. Filled-Epon Centrifuges are made from an ~~ep~~ epoxy resin with a filler consisting of a powdered aluminium ~~or powdered charcoal~~. The ~~filler~~ aluminium

ALUMINIUM

~~filler~~ increases the strength and thermal conductivity of Epon, while the powdered charcoal simply makes the ~~filler~~ epoxy opaque.

However, there is still a possibility of aluminium ions contaminating the sample particularly after repeated use of the centrifuge. To avoid this, aluminium-filled Epon centrifuges are subjected to a passivation process in which they are soaked in a 20% solution of sodium hydroxide. This process removes aluminium particles from the centrifuge surfaces.

After machining, the aluminium-filled Epon centrifuges are subjected to a passivation process in which they are soaked in a 20% solution of sodium hydroxide. This process removes aluminium particles from the centrifuge surfaces.

Filled-Epon centrifuges <sup>are used</sup> for aqueous solutions in the pH range of 3 to 10. They are the most widely used and recommended for biological materials. ~~The Epon is mixed with either powdered aluminium or powder~~

The water absorption of filled-Epon is negligible. Some reagents, however, may penetrate the centrifuge and soften it slightly. Generally, any softening effect can be eliminated by rinsing the centrifuge with distilled water after run, regardless of what material was run. The following chemicals

If this possibility can affect the results of an experiment, or if results suggest that it is having an effect, charcoal-filled Epon centrifuges should be used.

cause excess softening of films - Egm and should not be used with this centre piece:

Acetic acid, glacial

Ammonium hydroxide (27.1%)

Chloroform

Diethylene triamine

Dimethyl ~~sulph~~ <sup>sulph</sup> oxide

Ethylene diamine

Formaldehyde (40.1%)

M-Cresol

N,N-dimethylformamide

Nitric acid (10.1%)

Phosphoric acid (85.1%)

Sulphuric acid (70.1%)

Tetrahydrofuran

The maximum <sup>operating</sup> speeds are: <sup>for</sup> single <sup>sector</sup> sectors - maximum speed of rotor, for double sectors - 50,000 rpm, for single-sector capillary - 60,000 rpm, for 6-channel equilibrium - 48,000 rpm and for interference wedges - 44,000 rpm. The maximum operating deflection is  $40^\circ$ .

Aluminium Aluminium is the strongest of the centrifuge materials, has the best resistance to temperature and has the longest life expectancy. Aluminium centrifuges are recommended primarily for non-biological materials and for high temperature work. ~~Standard single~~ Solutions in aluminium centrifuges must be kept at the neutral pH range, and some of the organic solvents that plastics do not tolerate can be used. For protection against corrosion, each aluminium centrifuge is anodized. The hard, anodized surface permits the use of aluminium centrifuges with a wide variety of materials. When handling these centrifuges, care must be taken not to scratch the anodized surface, for corrosion can begin in the ~~scratches~~ ~~at~~ scratches on the finish.

Table IA classifies the groups of chemicals according to their effect on aluminium centrifuges while Table IB is a partial list of individual chemicals corrosive to aluminium centrifuges, (copy Tables 2D & 2E from Beckman booklet p. 29.)

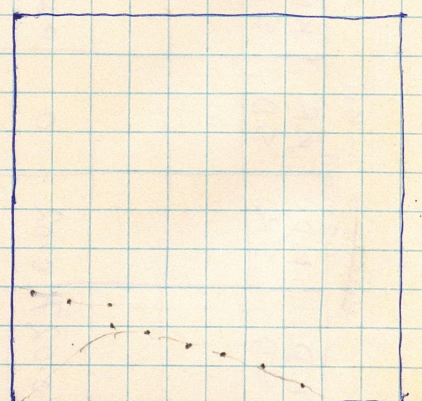
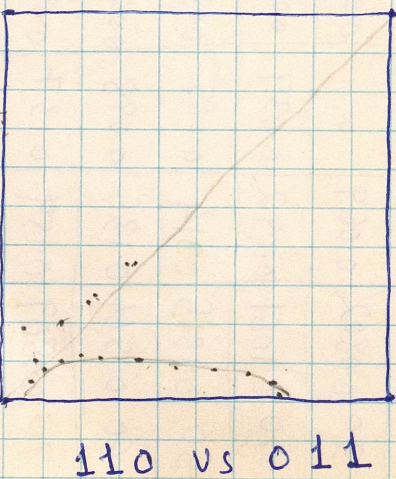
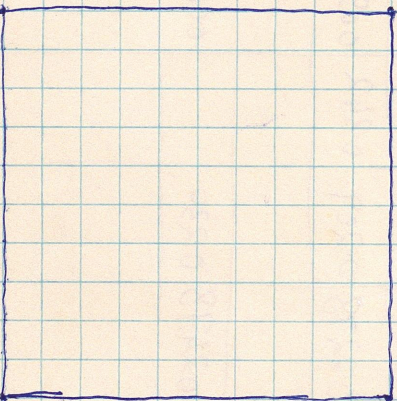
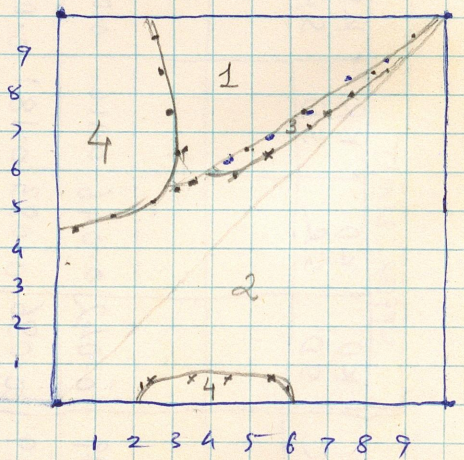
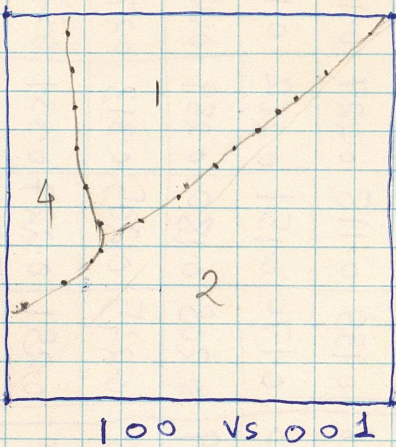
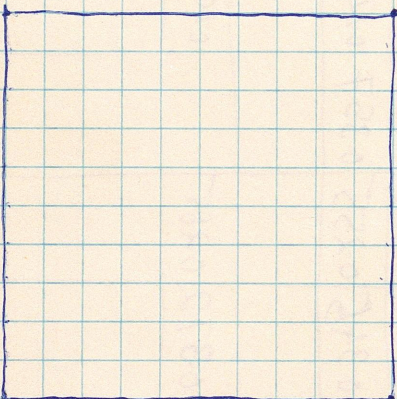
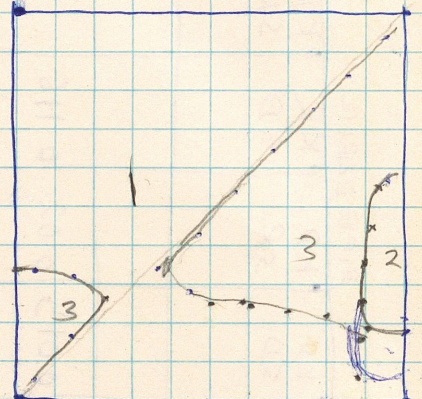
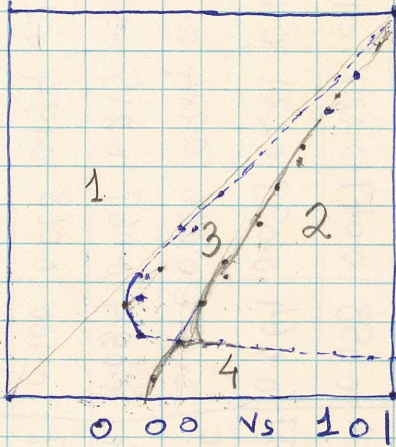
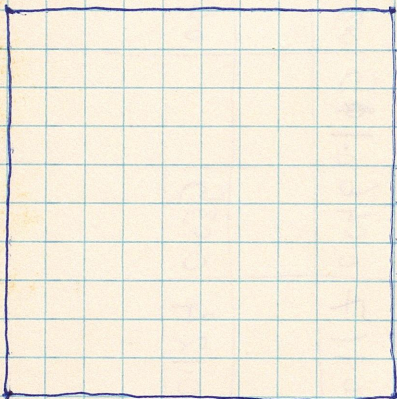
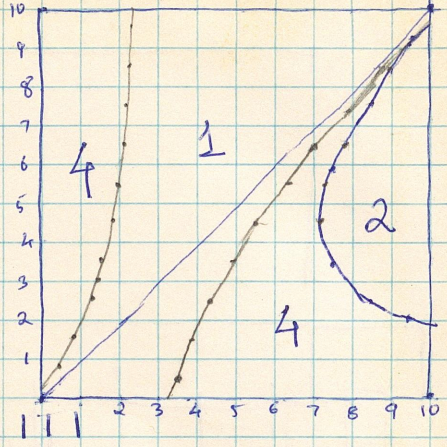
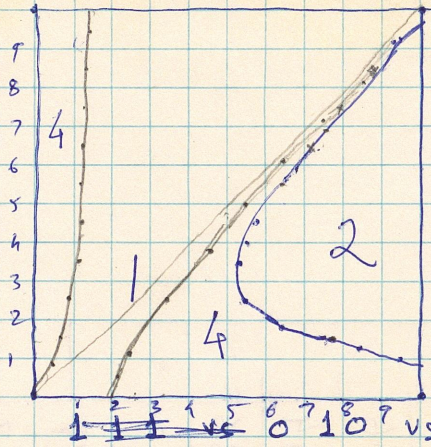
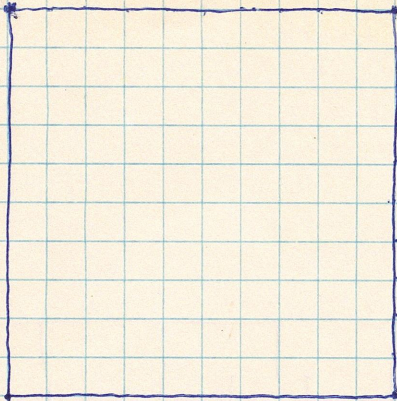


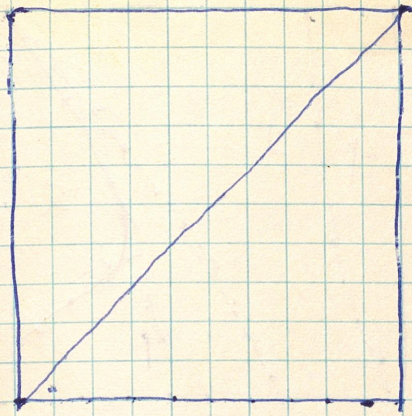
150

$d=0.10$

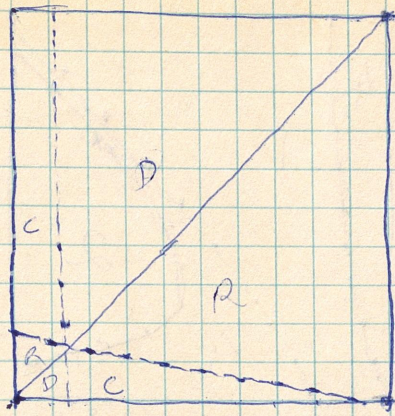
$d=0.50$

$d=0.90$



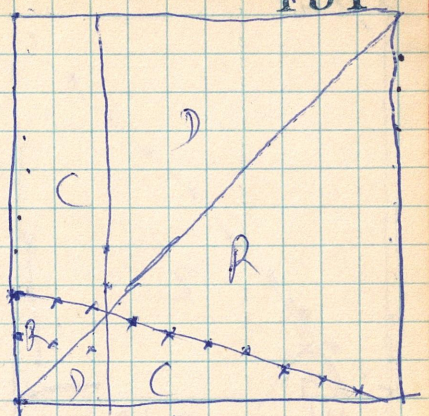


$d=0.1$



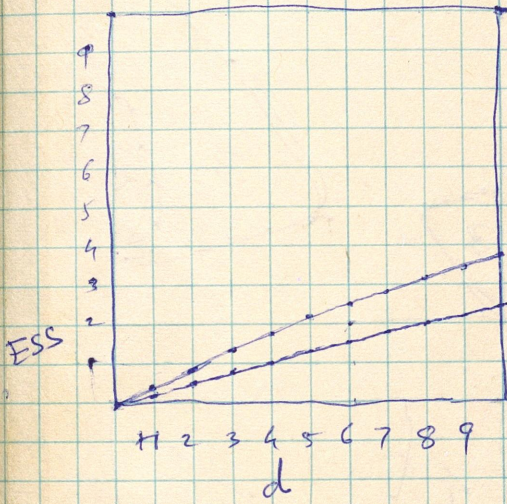
2,1,1 vs 2,1,0

$d=0.5$

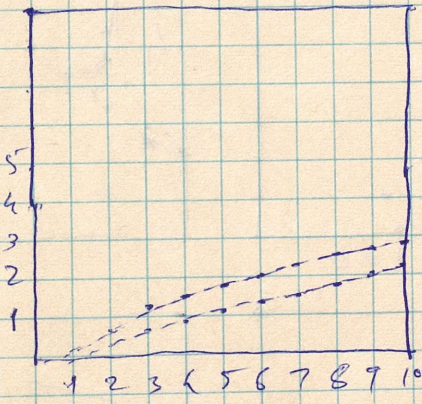
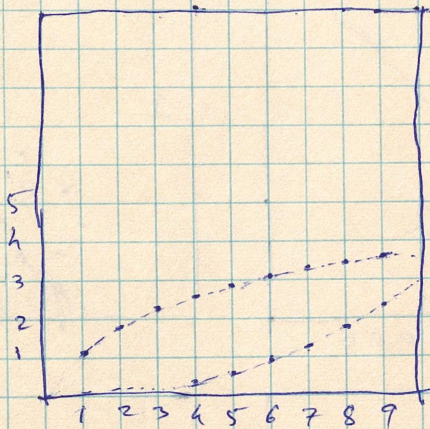


$d=0.9$

010 vs 111



000 vs 101



011 vs 110

152  $d=0.1$

$d=0.5$

$d=0.9$

